
**Information Technology —
Programming languages, their
environments, and system software
interfaces — Floating-point
extensions for C —**

**Part 4:
Supplementary functions**

*Technologies de l'information — Langages de programmation, leurs
environnements et interfaces du logiciel système — Extensions à
virgule flottante pour C —*

Partie 4: Fonctions supplémentaires

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Foreword

ISO (the International Organization for Standardization) and IEC (the International Electrotechnical Commission) form the specialized system for worldwide standardization. National bodies that are members of ISO or IEC participate in the development of International Standards through technical committees established by the respective organization to deal with particular fields of technical activity. ISO and IEC technical committees collaborate in fields of mutual interest. Other international organizations, governmental and non-governmental, in liaison with ISO and IEC, also take part in the work. In the field of information technology, ISO and IEC have established a joint technical committee, ISO/IEC JTC 1.

The procedures used to develop this document and those intended for its further maintenance are described in the ISO/IEC Directives, Part 1. In particular the different approval criteria needed for the different types of document should be noted. This document was drafted in accordance with the editorial rules of the ISO/IEC Directives, Part 2 (see www.iso.org/directives).

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The committee responsible for this document is ISO/IEC JTC 1, *Information technology*, Subcommittee SC 22, *Programming languages, their environments, and system software interfaces*.

ISO/IEC TS 18661 consists of the following parts, under the general title *Information technology — Programming languages, their environments, and system software interfaces — Floating-point extensions for C*:

- *Part 1: Binary floating-point arithmetic*
- *Part 2: Decimal floating-point arithmetic*
- *Part 3: Interchange and extended types*
- *Part 4: Supplementary functions*

The following part is under preparation:

- *Part 5: Supplementary attributes*

ISO/IEC TS 18661-1 updates ISO/IEC 9899:2011, *Information technology — Programming Language C*, annex F in particular, to support all required features of ISO/IEC/IEEE 60559:2011, *Information technology — Microprocessor Systems — Floating-point arithmetic*.

ISO/IEC TS 18661-2 supersedes ISO/IEC TR 24732:2009, *Information technology — Programming languages, their environments and system software interfaces — Extension for the programming language C to support decimal floating-point arithmetic*.

ISO/IEC TS 18661-3, ISO/IEC TS 18661-4, and ISO/IEC TS 18661-5 specify extensions to ISO/IEC 9899:2011 for features recommended in ISO/IEC/IEEE 60559:2011.

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Introduction

Background

IEC 60559 floating-point standard

The IEEE 754-1985 standard for binary floating-point arithmetic was motivated by an expanding diversity in floating-point data representation and arithmetic, which made writing robust programs, debugging, and moving programs between systems exceedingly difficult. Now the great majority of systems provide data formats and arithmetic operations according to this standard. The IEC 60559:1989 international standard was equivalent to the IEEE 754-1985 standard. Its stated goals were the following:

- 1 Facilitate movement of existing programs from diverse computers to those that adhere to this standard.
- 2 Enhance the capabilities and safety available to programmers who, though not expert in numerical methods, may well be attempting to produce numerically sophisticated programs. However, we recognize that utility and safety are sometimes antagonists.
- 3 Encourage experts to develop and distribute robust and efficient numerical programs that are portable, by way of minor editing and recompilation, onto any computer that conforms to this standard and possesses adequate capacity. When restricted to a declared subset of the standard, these programs should produce identical results on all conforming systems.
- 4 Provide direct support for
 - a. Execution-time diagnosis of anomalies
 - b. Smoother handling of exceptions
 - c. Interval arithmetic at a reasonable cost
- 5 Provide for development of
 - a. Standard elementary functions such as exp and cos
 - b. Very high precision (multiword) arithmetic
 - c. Coupling of numerical and symbolic algebraic computation
- 6 Enable rather than preclude further refinements and extensions.

To these ends, the standard specified a floating-point model comprising the following:

- *formats* – for binary floating-point data, including representations for Not-a-Number (NaN) and signed infinities and zeros
- *operations* – basic arithmetic operations (addition, multiplication, etc.) on the format data to compose a well-defined, closed arithmetic system; also specified conversions between floating-point formats and decimal character sequences, and a few auxiliary operations
- *context* – status flags for detecting exceptional conditions (invalid operation, division by zero, overflow, underflow, and inexact) and controls for choosing different rounding methods

The ISO/IEC/IEEE 60559:2011 international standard is equivalent to the IEEE 754-2008 standard for floating-point arithmetic, which is a major revision to IEEE 754-1985.

The revised standard specifies more formats, including decimal as well as binary. It adds a 128-bit binary format to its basic formats. It defines extended formats for all of its basic formats. It specifies data interchange formats (which may or may not be arithmetic), including a 16-bit binary format and an unbounded tower of wider formats. To conform to the floating-point standard, an implementation must provide at least one of the basic formats, along with the required operations.

The revised standard specifies more operations. New requirements include – among others – arithmetic operations that round their result to a narrower format than the operands (with just one rounding), more conversions with integer types, more classifications and comparisons, and more operations for managing flags and modes. New recommendations include an extensive set of mathematical functions and seven reduction functions for sums and scaled products.

The revised standard places more emphasis on reproducible results, which is reflected in its standardization of more operations. For the most part, behaviors are completely specified. The standard requires conversions between floating-point formats and decimal character sequences to be correctly rounded for at least three more decimal digits than is required to distinguish all numbers in the widest supported binary format; it fully specifies conversions involving any number of decimal digits. It recommends that transcendental functions be correctly rounded.

The revised standard requires a way to specify a constant rounding direction for a static portion of code, with details left to programming language standards. This feature potentially allows rounding control without incurring the overhead of runtime access to a global (or thread) rounding mode.

Other features recommended by the revised standard include alternate methods for exception handling, controls for expression evaluation (allowing or disallowing various optimizations), support for fully reproducible results, and support for program debugging.

The revised standard, like its predecessor, defines its model of floating-point arithmetic in the abstract. It neither defines the way in which operations are expressed (which might vary depending on the computer language or other interface being used), nor does it define the concrete representation (specific layout in storage, or in a processor's register, for example) of data or context, except that it does define specific encodings that are to be used for the exchange of floating-point data between different implementations that conform to the specification.

IEC 60559 does not include bindings of its floating-point model for particular programming languages. However, the revised standard does include guidance for programming language standards, in recognition of the fact that features of the floating-point standard, even if well supported in the hardware, are not available to users unless the programming language provides a commensurate level of support. The implementation's combination of both hardware and software determines conformance to the floating-point standard.

C support for IEC 60559

The C standard specifies floating-point arithmetic using an abstract model. The representation of a floating-point number is specified in an abstract form where the constituent components (sign, exponent, significand) of the representation are defined but not the internals of these components. In particular, the exponent range, significand size, and the base (or radix) are implementation-defined. This allows flexibility for an implementation to take advantage of its underlying hardware architecture. Furthermore, certain behaviors of operations are also implementation-defined, for example in the area of handling of special numbers and in exceptions.

The reason for this approach is historical. At the time when C was first standardized, before the floating-point standard was established, there were various hardware implementations of floating-point arithmetic in common use. Specifying the exact details of a representation would have made most of the existing implementations at the time not conforming.

Beginning with ISO/IEC 9899:1999 (C99), C has included an optional second level of specification for implementations supporting the floating-point standard. C99, in conditionally normative annex F, introduced nearly complete support for the IEC 60559:1989 standard for binary floating-point arithmetic. Also, C99's informative annex G offered a specification of complex arithmetic that is compatible with IEC 60559:1989.

ISO/IEC 9899:2011 (C11) includes refinements to the C99 floating-point specification, though it is still based on IEC 60559:1989. C11 upgraded annex G from “informative” to “conditionally normative”.

ISO/IEC TR 24732:2009 introduced partial C support for the decimal floating-point arithmetic in ISO/IEC/IEEE 60559:2011. ISO/IEC TR 24732, for which technical content was completed while IEEE 754-2008 was still in the later stages of development, specifies decimal types based on ISO/IEC/IEEE 60559:2011 decimal formats, though it does not include all of the operations required by ISO/IEC/IEEE 60559:2011.

Purpose

The purpose of ISO/IEC TS 18661 is to provide a C language binding for ISO/IEC/IEEE 60559:2011, based on the C11 standard, that delivers the goals of ISO/IEC/IEEE 60559 to users and is feasible to implement. It is organized into five parts.

ISO/IEC TS 18661-1 provides changes to C11 that cover all the requirements, plus some basic recommendations, of ISO/IEC/IEEE 60559:2011 for binary floating-point arithmetic. C implementations intending to support ISO/IEC/IEEE 60559:2011 are expected to conform to conditionally normative annex F as enhanced by the changes in ISO/IEC TS 18661-1.

ISO/IEC TS 18661-2 enhances ISO/IEC TR 24732 to cover all the requirements, plus some basic recommendations, of ISO/IEC/IEEE 60559:2011 for decimal floating-point arithmetic. C implementations intending to provide an extension for decimal floating-point arithmetic supporting ISO/IEC/IEEE 60559:2011 are expected to conform to ISO/IEC TS 18661-2.

ISO/IEC TS 18661-3 (Interchange and extended types), ISO/IEC TS 18661-4 (Supplementary functions), and ISO/IEC TS 18661-5 (Supplementary attributes) cover recommended features of ISO/IEC/IEEE 60559:2011. C implementations intending to provide extensions for these features are expected to conform to the corresponding parts.

Additional background on supplementary functions

This document uses the term supplementary functions to refer to functions that provide operations recommended, but not required, by IEC 60559.

ISO/IEC/IEEE 60559:2011 specifies and recommends a more extensive set of mathematical operations than C11 provides. The IEC 60559 specification is generally consistent with C11, though it adds requirements for symmetry and antisymmetry. This part of ISO/IEC TS 18661 extends the specification in Library subclause 7.12 Mathematics to include the complete set of IEC 60559 mathematical operations. For implementations conforming to annex F, it also requires full IEC 60559 semantics, including symmetry and antisymmetry properties.

IEC 60559 requires correct rounding for its required operations (squareRoot, fusedMultiplyAdd, etc.), and recommends correct rounding for its recommended mathematical operations. This part of ISO/IEC TS 18661 reserves identifiers, with **cr** prefixes, for C functions corresponding to correctly rounded versions of the IEC 60559 mathematical operations, which may be provided at the option of the implementation. For example, the identifier **crexp** is reserved for a correctly rounded version of the **exp** function.

IEC 60559 also specifies and recommends reduction operations, which operate on vector operands. These operations, which compute sums and products, may associate in any order and may evaluate in any wider format. Hence, unlike other IEC 60559 operations, they do not have unique specified results. This part of ISO/IEC TS 18661 extends the specification in Library subclause 7.12 Mathematics to include functions corresponding to the IEC 60559 reduction operations. For implementations conforming to annex F, it also requires the IEC 60559 specified behavior for floating-point exceptions.

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Information technology — Programming languages, their environments, and system software interfaces — Floating-point extensions for C —

Part 4: Supplementary functions

1 Scope

This part of ISO/IEC TS 18661 extends programming language C to include functions specified and recommended in ISO/IEC/IEEE 60559:2011.

2 Conformance

An implementation conforms to this part of ISO/IEC TS 18661 if

- a) it meets the requirements for a conforming implementation of C11 with all the changes to C11 as specified in parts 1-4 of ISO/IEC TS 18661;
- b) it conforms to ISO/IEC TS 18661-1 or ISO/IEC TS 18661-2 (or both); and
- c) it defines `__STDC_IEC_60559_FUNCS__` to `201506L`.

3 Normative references

The following documents, in whole or in part, are normatively referenced in this document and are indispensable for its application. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO/IEC 9899:2011, *Information technology — Programming languages — C*

ISO/IEC/IEEE 60559:2011, *Information technology — Microprocessor Systems — Floating-point arithmetic*

ISO/IEC TS 18661-1:2014, *Information technology — Programming languages, their environments and system software interfaces — Floating-point extensions for C — Part 1: Binary floating-point arithmetic*

ISO/IEC TS 18661-2:2015, *Information technology — Programming languages, their environments and system software interfaces — Floating-point extensions for C — Part 2: Decimal floating-point arithmetic*

ISO/IEC TS 18661-3:2015, *Information technology — Programming languages, their environments and system software interfaces — Floating-point extensions for C — Part 3: Interchange and extended types*

4 Terms and definitions

For the purposes of this document, the terms and definitions given in ISO/IEC 9899:2011, ISO/IEC/IEEE 60559:2011, ISO/IEC TS 18661-1:2014, ISO/IEC TS 18661-2:2015, ISO/IEC TS 18661-3:2015, and the following apply.

4.1

C11

standard ISO/IEC 9899:2011, *Information technology — Programming languages C*, including *Technical Corrigendum 1* (ISO/IEC 9899:2011/Cor. 1:2012)

5 C standard conformance

5.1 Freestanding implementations

The specification in C11 + TS18661-1 + TS18661-2 allows freestanding implementations to conform to this part of ISO/IEC TS 18661.

5.2 Predefined macros

Change to C11 + TS18661-1 + TS18661-2 + TS18661-3:

In 6.10.8.3#1, add:

__STDC_IEC_60559_FUNCS__ The integer constant **201506L**, intended to indicate support of functions specified and recommended in IEC 60559.

5.3 Standard headers

The new identifiers added to C11 library headers by this Part of Technical Specification 18661 are defined or declared by their respective headers only if **__STDC_WANT_IEC_60559_FUNCS_EXT__** is defined as a macro at the point in the source file where the appropriate header is first included. The following changes to C11 + TS18661-1 + TS18661-2 + TS18661-3 list these identifiers in each applicable library subclause.

Changes to C11 + TS18661-1 + TS18661-2 + TS18661-3:

In 7.12, renumber paragraph 1e to 1h, and after paragraph 1d insert the paragraphs:

[1e] The following identifiers are declared only if **__STDC_WANT_IEC_60559_FUNCS_EXT__** is defined as a macro at the point in the source file where **<math.h>** is first included:

exp2m1	rootnf	sinpil
exp2m1f	rootnl	tanpi
exp2m1l	pown	tanpif
exp10	pownf	tanpil
exp10f	pownl	reduc_sum
exp10l	powr	reduc_sumf
exp10m1	powrf	reduc_suml
exp10m1f	powrl	reduc_sumabs
exp10m1l	acospi	reduc_sumabsf
logp1	acospif	reduc_sumabsl
logp1f	acospil	reduc_sumsq

logp1l	asinpi	reduc_sumsqf
log2p1	asinpif	reduc_sumsq1
log2p1f	asinpil	reduc_sumprod
log2p1l	atanpi	reduc_sumprodf
log10p1	atanpif	reduc_sumprodl
log10p1f	atanpil	scaled_prod
log10p1l	atan2pi	scaled_prodf
rsqrt	atan2pif	scaled_prodl
rsqrtf	atan2pil	scaled_prodsum
rsqrtl	cospi	scaled_prodsumf
compoundn	cospif	scaled_prodsuml
compoundnf	cospil	scaled_proddiff
compoundnl	sinpi	scaled_proddiff1
rootn	sinpif	scaled_proddiff1

[1f] The following identifiers are declared only if `__STDC_WANT_IEC_60559_DFP_EXT__` and `__STDC_WANT_IEC_60559_FUNCS_EXT__` are defined as macros at the point in the source file where `<math.h>` is first included:

for supported types `__DecimalN`, where N = 32, 64, and 128:

exp2m1dN	powndN	tanpidN
exp10dN	powrdN	reduc_sumdN
exp10m1dN	acospidN	reduc_sumabsdN
logp1dN	asinpidN	reduc_sumsqdN
log2p1dN	atanpidN	reduc_sumproddN
log10p1dN	atan2pidN	scaled_proddN
rsqrtNdN	cospidN	scaled_prodsumdN
compoundndN	sinpidN	scaled_proddiffdN
rootndN		

[1g] The following identifiers are declared only if `__STDC_WANT_IEC_60559_TYPES_EXT__` and `__STDC_WANT_IEC_60559_FUNCS_EXT__` are defined as macros at the point in the source file where `<math.h>` is first included:

for supported types `__FloatN`:

exp2m1fN	pownfN	tanpifN
exp10fN	powrfN	reduc_sumfN
exp10m1fN	acospifN	reduc_sumabsfN
logp1fN	asinpifN	reduc_sumsqfN
log2p1fN	atanpifN	reduc_sumprodfN
log10p1fN	atan2pifN	scaled_prodfN
rsqrtfN	cospifN	scaled_prodsumfN
compoundnfN	sinpifN	scaled_proddiffN
rootnfN		

for supported types **_FloatNx**:

exp2m1fNx	pownfNx	tanpifNx
exp10fNx	powrfNx	reduc_sumfNx
exp10m1fNx	acospifNx	reduc_sumabsfNx
logp1fNx	asinpifNx	reduc_sumsqfNx
log2p1fNx	atanpifNx	reduc_sumprodfNx
log10p1fNx	atan2pifNx	scaled_prodfNx
rsqrtfNx	cospifNx	scaled_prodsumfNx
compoundnfNx	sinpifNx	scaled_proddiffNx
rootnfNx		

for supported types **_DecimalN**, where $N \neq 32, 64$, and 128:

exp2m1dN	powndN	tanpidN
exp10dN	powrdN	reduc_sumdN
exp10m1dN	acospidN	reduc_sumabsdN
logp1dN	asinp1dN	reduc_sumsqdN
log2p1dN	atanpidN	reduc_sumproddN
log10p1dN	atan2pidN	scaled_proddN
rsqrt1dN	cospidN	scaled_prodsumdN
compoundndN	sinpidN	scaled_proddiffdN
rootndN		

for supported types **_DecimalNx**:

exp2m1dNx	powndNx	tanpidNx
exp10dNx	powrdNx	reduc_sumdNx
exp10m1dNx	acospidNx	reduc_sumabsdNx
logp1dNx	asinp1dNx	reduc_sumsqdNx
log2p1dNx	atanpidNx	reduc_sumproddNx
log10p1dNx	atan2pidNx	scaled_proddNx
rsqrt1dNx	cospidNx	scaled_prodsumdNx
compoundndNx	sinpidNx	scaled_proddiffdNx
rootndNx		

After 7.25#1c, insert the paragraph:

[1d] The following identifiers are defined as type-generic macros only if **__STDC_WANT_IEC_60559_FUNCS_EXT** is defined as a macro at the point in the source file where **<tgmath.h>** is first included:

exp2m1	rsqrt	asinpi
exp10	compoundn	atanpi
exp10m1	rootn	atan2pi
logp1	pown	cosp1
log2p1	powr	sinpi
log10p1	acosp1	tanpi

6 Operation binding

The following change to C11 + TS18661-1 + TS18661-2 + TS18661-3 shows how functions in C11 and in this Part of Technical Specification 18661 provide operations recommended in IEC 60559.

Change to C11 + TS18661-1 + TS18661-2 + TS18661-3:

After F.3#22, add:

[23] The C functions in the following table provide operations recommended by IEC 60559 and similar operations. Correct rounding, which IEC 60559 specifies for its operations (except for the reduction operations), is not required for the C functions in the table. See also 7.31.6a.

IEC 60559 operation	C function	Clauses - C11
exp	exp	7.12.6.1, F.10.3.1
expm1	expm1	7.12.6.3, F.10.3.3
exp2	exp2	7.12.6.2, F.10.3.2
exp2m1	exp2m1	7.12.6.14, F.10.3.14
exp10	exp10	7.12.6.15, F.10.3.15
exp10m1	exp10m1	7.12.6.16, F.10.3.16
log	log	7.12.6.7, F.10.3.7
log2	log2	7.12.6.10, F.10.3.10
log10	log10	7.12.6.8, F.10.3.8
logp1	log1p, logp1	7.12.6.9, F.10.3.9
log2p1	log2p1	7.12.6.17, F.10.3.17
log10p1	log10p1	7.12.6.18, F.10.3.18
hypot	hypot	7.12.7.3, F.10.4.3
rSqrt	rsqrt	7.12.7.6, F.10.4.6
compound	compoundn	7.12.7.7, F.10.4.7
rootn	rootn	7.12.7.8, F.10.4.8
pown	pown	7.12.7.9, F.10.4.9
pow	pow	7.12.7.4, F.10.4.4
powr	powr	7.12.7.10, F.10.4.10
sin	sin	7.12.4.6, F.10.1.6
cos	cos	7.12.4.5, F.10.1.5
tan	tan	7.12.4.7, F.10.1.7
sinPi	sinpi	7.12.4.13, F.10.1.13
cosPi	cospi	7.12.4.12, F.10.1.12
	tanpi	7.12.4.14, F.10.1.14
	asinpi	7.12.4.9, F.10.1.9
	acospi	7.12.4.8, F.10.1.8
atanPi	atanpi	7.12.4.10, F.10.1.10
atan2Pi	atan2pi	7.12.4.11, F.10.1.11
asin	asin	7.12.4.2, F.10.1.2
acos	acos	7.12.4.1, F.10.1.1
atan	atan	7.12.4.3, F.10.1.3
atan2	atan2	7.12.4.4, F.10.1.4
sinh	sinh	7.12.5.5, F.10.2.5
cosh	cosh	7.12.5.4, F.10.2.4
tanh	tanh	7.12.5.6, F.10.2.6
asinh	asinh	7.12.5.2, F.10.2.2
acosh	acosh	7.12.5.1, F.10.2.1

atanh	atanh	7.12.5.3, F.10.2.3
sum	reduc_sum	7.12.13b.1, F.10.10b.1
dot	reduc_sumprod	7.12.13b.4, F.10.10b.4
sumSquare	reduc_sumsq	7.12.13b.3, F.10.10b.3
sumAbs	reduc_sumabs	7.12.13b.2, F.10.13b.2
scaledProd	scaled_prod	7.12.13b.5, F.10.10b.5
scaledProdSum	scaled_prodsum	7.12.13b.6, F.10.10b.6
scaledProdDiff	scaled_proddiff	7.12.13b.7, F.10.10b.7

7 Mathematical functions in <math.h>

This clause specifies changes to C11 + TS18661-1 + TS18661-2 + TS18661-3 to include functions that support mathematical operations recommended by IEC 60559. The changes reserve names for correctly rounded versions of the functions. IEC 60559 recommends support for the correctly rounded functions. The changes also support the symmetry and antisymmetry properties that IEC 60559 specifies for mathematical functions.

After 7.12.4.7, insert the following:

7.12.4.8 The **acospi** functions

Synopsis

```
[1] #include <math.h>
double acospi(double x);
float acospif(float x);
long double acospil(long double x);
_FloatN acospifN(_FloatN x);
_FloatNx acospifNx(_FloatNx x);
_DecimalN acospidN(_DecimalN x);
_DecimalNx acospidNx(_DecimalNx x);
```

Description

[2] The **acospi** functions compute the principal value of the arc cosine of x , divided by π , thus measuring the angle in half-revolutions. A domain error occurs for arguments not in the interval $[-1, +1]$.

Returns

[3] The **acospi** functions return $\arccos(x)/\pi$, in the interval $[0, 1]$.

7.12.4.9 The **asinpi** functions

Synopsis

```
[1] #include <math.h>
double asinpi(double x);
float asinpif(float x);
long double asinpil(long double x);
_FloatN asinpifN(_FloatN x);
_FloatNx asinpifNx(_FloatNx x);
_DecimalN asinpidN(_DecimalN x);
_DecimalNx asinpidNx(_DecimalNx x);
```

Description

[2] The **asinpi** functions compute the principal value of the arc sine of **x**, divided by π , thus measuring the angle in half-revolutions. A domain error occurs for arguments not in the interval $[-1, +1]$. A range error occurs if the magnitude of nonzero **x** is too small.

Returns

[3] The **asinpi** functions return $\arcsin(\mathbf{x}) / \pi$, in the interval $[-1/2, +1/2]$.

7.12.4.10 The **atanpi** functions

Synopsis

```
[1] #include <math.h>
double atanpi(double x);
float atanpif(float x);
long double atanpil(long double x);
_FloatN atanpifN(_FloatN x);
_FloatNx atanpifNx(_FloatNx x);
_DecimalN atanpidN(_DecimalN x);
_DecimalNx atanpidNx(_DecimalNx x);
```

Description

[2] The **atanpi** functions compute the principal value of the arc tangent of **x**, divided by π , thus measuring the angle in half-revolutions. A range error occurs if the magnitude of nonzero **x** is too small.

Returns

[3] The **atanpi** functions return $\arctan(\mathbf{x}) / \pi$, in the interval $[-1/2, +1/2]$.

7.12.4.11 The **atan2pi** functions

Synopsis

```
[1] #include <math.h>
double atan2pi(double y, double x);
float atan2pif(float y, float x);
long double atan2pil(long double y, long double x);
_FloatN atan2pifN(_FloatN y, _FloatN x);
_FloatNx atan2pifNx(_FloatNx y, _FloatNx x);
_DecimalN atan2pidN(_DecimalN y, _DecimalN x);
_DecimalNx atan2pidNx(_DecimalNx y, _DecimalNx x);
```

Description

[2] The **atan2pi** functions compute the angle, measured in half-revolutions, subtended at the origin by the point (**x**, **y**) and the positive *x*-axis. Thus, **atan2pi** computes $\arctan(y/x) / \pi$, in the range $[-1, +1]$. A domain error may occur if both arguments are zero. A range error occurs if **x** is positive and the magnitude of nonzero **y/x** is too small.

Returns

[3] The **atan2pi** functions return the computed angle, in the interval $[-1, +1]$.

7.12.4.12 The **cosp** functions

Synopsis

```
[1] #include <math.h>
double cosp(double x);
float cospif(float x);
long double cospil(long double x);
_FloatN cospifN(_FloatN x);
_FloatNx cospifNx(_FloatNx x);
_DecimalN cospidN(_DecimalN x);
_DecimalNx cospidNx(_DecimalNx x);
```

Description

[2] The **cosp** functions compute the cosine of $\pi \times x$, thus regarding **x** as a measurement in half-revolutions.

Returns

[3] The **cosp** functions return $\cos(\pi \times x)$.

7.12.4.13 The **sinpi** functions

Synopsis

```
[1] #include <math.h>
double sinpi(double x);
float sinpif(float x);
long double sinpil(long double x);
_FloatN sinpifN(_FloatN x);
_FloatNx sinpifNx(_FloatNx x);
_DecimalN sinpidN(_DecimalN x);
_DecimalNx sinpidNx(_DecimalNx x);
```

Description

[2] The **sinpi** functions compute the sine of $\pi \times x$, thus regarding x as a measurement in half-revolutions.

Returns

[3] The **sinpi** functions return $\sin(\pi \times x)$.

7.12.4.14 The **tanpi** functions

Synopsis

```
[1] #include <math.h>
double tanpi(double x);
float tanpif(float x);
long double tanpil(long double x);
_FloatN tanpifN(_FloatN x);
_FloatNx tanpifNx(_FloatNx x);
_DecimalN tanpidN(_DecimalN x);
_DecimalNx tanpidNx(_DecimalNx x);
```

Description

[2] The **tanpi** functions compute the tangent of $\pi \times x$, thus regarding x as a measurement in half-revolutions. A pole error may occur for arguments $n + 1/2$, for integers n .

Returns

[3] The **tanpi** functions return $\tan(\pi \times x)$.

In 7.12.6.9, replace the subclause title:

7.12.6.9 The **log1p** functions

with:

7.12.6.9 The **log1p** and **logp1** functions

In 7.12.6.9#1, append to the Synopsis:

```
double logp1(double x);
float logp1f(float x);
long double logp1l(long double x);
_FloatN logp1fN(_FloatN x);
_FloatNx logp1fNx(_FloatNx x);
_DecimalN logp1dN(_DecimalN x);
_DecimalNx logp1dNx(_DecimalNx x);
```

In 7.12.6.9#2, replace the first sentence:

The **log1p** functions compute the base-*e* (natural) logarithm of 1 plus the argument.

with:

The **log1p** functions are equivalent to the **logp1** functions. These functions compute the base-*e* (natural) logarithm of 1 plus the argument.

Replace 7.12.6.9#3:

[3] The **log1p** functions return $\log_e (1 + x)$.

with:

[3] These functions return $\log_e (1 + x)$.

In F.10.3.9, replace the subclause title:

F.10.3.9 The **log1p** functions

with:

F.10.3.9 The **log1p** and **logp1** functions

After 7.12.6.13, insert the following:

7.12.6.14 The **exp2m1** functions

Synopsis

```
[1] #include <math.h>
double exp2m1(double x);
float exp2m1f(float x);
long double exp2m1l(long double x);
_FloatN exp2m1fN(_FloatN x);
_FloatNx exp2m1fNx(_FloatNx x);
_DecimalN exp2m1dN(_DecimalN x);
_DecimalNx exp2m1dNx(_DecimalNx x);
```

Description

[2] The **exp2m1** functions compute the base-2 exponential of the argument, minus 1. A range error occurs if finite **x** is too large or if the magnitude of nonzero **x** is too small.

Returns

[3] The **exp2m1** functions return $2^x - 1$.

7.12.6.15 The exp10 functions**Synopsis**

```
[1] #include <math.h>
double exp10(double x);
float exp10f(float x);
long double exp10l(long double x);
_FloatN exp10fN(_FloatN x);
_FloatNx exp10fNx(_FloatNx x);
_DecimalN exp10dN(_DecimalN x);
_DecimalNx exp10dNx(_DecimalNx x);
```

Description

[2] The **exp10** functions compute the base-10 exponential of the argument. A range error occurs if the magnitude of finite **x** is too large.

Returns

[3] The **exp10** functions return 10^x .

7.12.6.16 The exp10m1 functions**Synopsis**

```
[1] #include <math.h>
double exp10m1(double x);
float exp10m1f(float x);
long double exp10m1l(long double x);
_FloatN exp10m1fN(_FloatN x);
_FloatNx exp10m1fNx(_FloatNx x);
_DecimalN exp10m1dN(_DecimalN x);
_DecimalNx exp10m1dNx(_DecimalNx x);
```

Description

[2] The **exp10m1** functions compute the base-10 exponential of the argument, minus 1. A range error occurs if finite **x** is too large.

Returns

[3] The **exp10m1** functions return $10^x - 1$.

7.12.6.17 The **log2p1** functions

Synopsis

```
[1] #include <math.h>
double log2p1(double x);
float log2p1f(float x);
long double log2p1l(long double x);
_FloatN log2p1fN(_FloatN x);
_FloatNx log2p1fNx(_FloatNx x);
_DecimalN log2p1dN(_DecimalN x);
_DecimalNx log2p1dNx(_DecimalNx x);
```

Description

[2] The **log2p1** functions compute the base-2 logarithm of 1 plus the argument. A domain error occurs if the argument is less than -1. A pole error may occur if the argument equals -1.

Returns

[3] The **log2p1** functions return $\log_2(1 + x)$.

7.12.6.18 The **log10p1** functions

Synopsis

```
[1] #include <math.h>
double log10p1(double x);
float log10p1f(float x);
long double log10p1l(long double x);
_FloatN log10p1fN(_FloatN x);
_FloatNx log10p1fNx(_FloatNx x);
_DecimalN log10p1dN(_DecimalN x);
_DecimalNx log10p1dNx(_DecimalNx x);
```

Description

[2] The **log10p1** functions compute the base-10 logarithm of 1 plus the argument. A domain error occurs if the argument is less than -1. A pole error may occur if the argument equals -1. A range error occurs if the magnitude of nonzero x is too small.

Returns

[3] The **log10p1** functions return $\log_{10}(1 + x)$.

After 7.12.7.5, insert the following:

7.12.7.6 The **rsqrt** functions

Synopsis

```
[1] #include <math.h>
double rsqrt(double x);
float rsqrtf(float x);
long double rsqrtl(long double x);
_FloatN rsqrtfN(_FloatN x);
_FloatNx rsqrtfNx(_FloatNx x);
_DecimalN rsqrtndN(_DecimalN x);
_DecimalNx rsqrtndNx(_DecimalNx x);
```

Description

[2] The **rsqrt** functions compute the reciprocal of the square root of the argument. A domain error occurs if the argument is less than zero. A pole error may occur if the argument equals zero.

Returns

[3] The **rsqrt** functions return $1 / \sqrt{x}$.

7.12.7.7 The **compoundn** functions

Synopsis

```
[1] #include <math.h>
#include <stdint.h>
double compoundn(double x, intmax_t n);
float compoundnf(float x, intmax_t n);
long double compoundnl(long double x, intmax_t n);
_FloatN compoundnfN(_FloatN x, intmax_t n);
_FloatNx compoundnfNx(_FloatNx x, intmax_t n);
_DecimalN compoundndN(_DecimalN x, intmax_t n);
_DecimalNx compoundndNx(_DecimalNx x, intmax_t n);
```

Description

[2] The **compoundn** functions compute 1 plus **x**, raised to the power **n**. A domain error occurs if **x** < -1. A range error may occur if **n** is too large, depending on **x**. A pole error may occur if **x** equals -1 and **n** < 0.

Returns

[3] The functions return $(1 + x)^n$.

7.12.7.8 The **rootn** functions

Synopsis

```
[1] #include <math.h>
#include <stdint.h>
double rootn(double x, intmax_t n);
float rootnf(float x, intmax_t n);
long double rootnl(long double x, intmax_t n);
_FloattN rootnfN(_FloattN x, intmax_t n);
_FloattNx rootnfNx(_FloattNx x, intmax_t n);
_DecimalN rootndN(_DecimalN x, intmax_t n);
_DecimalNx rootndNx(_DecimalNx x, intmax_t n);
```

Description

[2] The **rootn** functions compute the principal **n**th root of **x**. A domain error occurs if **n** is 0 or if **x** < 0 and **n** is even. A range error may occur if **n** is -1. A pole error may occur if **x** equals zero and **n** < 0.

Returns

[3] The **rootn** functions return $x^{1/n}$.

7.12.7.9 The **pown** functions

Synopsis

```
[1] #include <math.h>
#include <stdint.h>
double pown(double x, intmax_t n);
float pownf(float x, intmax_t n);
long double pownl(long double x, intmax_t n);
_FloattN pownfN(_FloattN x, intmax_t n);
_FloattNx pownfNx(_FloattNx x, intmax_t n);
_DecimalN powndN(_DecimalN x, intmax_t n);
_DecimalNx powndNx(_DecimalNx x, intmax_t n);
```

Description

[2] The **pown** functions compute **x** raised to the **n**th power. A range error may occur. A pole error may occur if **x** equals zero and **n** < 0.

Returns

[3] The **pown** functions return x^n .

7.12.7.10 The **powr** functions

Synopsis

```
[1] #include <math.h>
double powr(double x, double y);
float powrf(float x, float y);
long double powrl(long double x, long double y);
_FloatNx powrfNx(_FloatNx x, _FloatNx y);
_FloatNx powrfNx(_FloatNx x, _FloatNx y);
_DecimalNx powrdNx(_DecimalNx x, _DecimalNx y);
_DecimalNx powrdNx(_DecimalNx x, _DecimalNx y);
```

Description

[2] The **powr** functions compute x raised to the power y as $\exp(y \times \log(x))$. A domain error occurs if $x < 0$ or if x and y are both zero. A range error may occur. A pole error may occur if x equals zero and finite $y < 0$.

Returns

[3] The **powr** functions return x^y .

After 7.31.6, insert:

7.31.6a Mathematics <math.h>

With the condition that the macro `__STDC_IEC_60559_FUNCS__` is defined, the function names

crexp	crsqrt	cracospi
crexpm1	crcompoundn	cratanpi
crexp2	crrootn	cratan2pi
crexp2m1	crpown	crasin
crexp10	crpow	cracos
crexp10m1	crpowr	cratan
crlog	crsin	cratan2
crlog2	crCOS	crsinh
crlog10	crtan	crCOSH
crlog1p	crsinpi	crtanh
crlogp1	crCOSpi	crasinh
crlog2p1	crtanpi	cracosh
crlog10p1	crasinpi	cratanh
crhypot		

and the same names suffixed with **f**, **l**, **fNx**, **dN**, or **dNx** may be added to the `<math.h>` header.

In 7.31.6a, attach a footnote to the wording:

With the condition that the macro `__STDC_IEC_60559_FUNCS__` is defined, the function names

where the footnote is:

*) The **cr** prefix is intended to indicate a correctly rounded version of the function.

After F.10#2, insert:

[2a] For each single-argument function f in **<math.h>** whose mathematical counterpart is symmetric (even), $f(x)$ is $f(-x)$ for all rounding modes and for all x in the (valid) domain of the function. For each single-argument function f in **<math.h>** whose mathematical counterpart is antisymmetric (odd), $f(-x)$ is $-f(x)$ for the IEC 60559 rounding modes `roundTiesToEven`, `roundTiesToAway`, and `roundTowardZero`, and for all x in the (valid) domain of the function. The **atan2** and **atan2pi** functions are odd in their first argument.

After F.10.1.7, insert the following:

F.10.1.8 The **acospi** functions

- **acospi**(+1) returns +0.
- **acospi**(x) returns a NaN and raises the “invalid” floating-point exception for $|x| > 1$.

F.10.1.9 The **asinpi** functions

- **asinpi**(± 0) returns ± 0 .
- **asinpi**(x) returns a NaN and raises the “invalid” floating-point exception for $|x| > 1$.

F.10.1.10 The **atanpi** functions

- **atanpi**(± 0) returns ± 0 .
- **atanpi**($\pm \infty$) returns $\pm 1/2$.

F.10.1.11 The **atan2pi** functions

- **atan2pi**($\pm 0, -0$) returns ± 1 .
- **atan2pi**($\pm 0, +0$) returns ± 0 .
- **atan2pi**($\pm 0, x$) returns ± 1 for $x < 0$.
- **atan2pi**($\pm 0, x$) returns ± 0 for $x > 0$.
- **atan2pi**($y, \pm 0$) returns $-1/2$ for $y < 0$.
- **atan2pi**($y, \pm 0$) returns $+1/2$ for $y > 0$.
- **atan2pi**($\pm y, -\infty$) returns ± 1 for finite $y > 0$.
- **atan2pi**($\pm y, +\infty$) returns ± 0 for finite $y > 0$.
- **atan2pi**($\pm \infty, x$) returns $\pm 1/2$ for finite x .
- **atan2pi**($\pm \infty, -\infty$) returns $\pm 3/4$ for finite x .
- **atan2pi**($\pm \infty, +\infty$) returns $\pm 1/4$ for finite x .

F.10.1.12 The **cospi** functions

- **cospi**(± 0) returns 1.
- **cospi**($n + 1/2$) returns +0, for integers n .
- **cospi**($\pm \infty$) returns a NaN and raises the “invalid” floating-point exception.

F.10.1.13 The $\sinpi$ functions

- $\sinpi(\pm 0)$ returns ± 0 .
- $\sinpi(\pm n)$ returns ± 0 , for positive integers n .
- $\sinpi(\pm\infty)$ returns a NaN and raises the “invalid” floating-point exception.

F.10.1.14 The $\tanpi$ functions

- $\tanpi(\pm 0)$ returns ± 0 .
- $\tanpi(n)$ returns $+0$, for positive even and negative odd integers n .
- $\tanpi(n)$ returns -0 , for positive odd and negative even integers n .
- $\tanpi(n + 1/2)$ returns $+\infty$ and raises the “divide-by-zero” floating-point exception, for even integers n .
- $\tanpi(n + 1/2)$ returns $-\infty$ and raises the “divide-by-zero” floating-point exception, for odd integers n .
- $\tanpi(\pm\infty)$ returns a NaN and raises the “invalid” floating-point exception.

After F.10.3.13, insert the following:

F.10.3.14 The $\exp2m1$ functions

- $\exp2m1(\pm 0)$ returns ± 0 .
- $\exp2m1(-\infty)$ returns -1 .
- $\exp2m1(+\infty)$ returns $+\infty$.

F.10.3.15 The $\exp10$ functions

- $\exp10(\pm 0)$ returns 1 .
- $\exp10(-\infty)$ returns $+0$.
- $\exp10(+\infty)$ returns $+\infty$.

F.10.3.16 The $\exp10m1$ functions

- $\exp10m1(\pm 0)$ returns ± 0 .
- $\exp10m1(-\infty)$ returns -1 .
- $\exp10m1(+\infty)$ returns $+\infty$.

F.10.3.17 The $\log2p1$ functions

- $\log2p1(\pm 0)$ returns ± 0 .
- $\log2p1(-1)$ returns $-\infty$ and raises the “divide-by-zero” floating-point exception.
- $\log2p1(x)$ returns a NaN and raises the “invalid” floating-point exception for $x < -1$.
- $\log2p1(+\infty)$ returns $+\infty$.

F.10.3.18 The $\log10p1$ functions

- $\log10p1(\pm 0)$ returns ± 0 .
- $\log10p1(-1)$ returns $-\infty$ and raises the “divide-by-zero” floating-point exception.
- $\log10p1(x)$ returns a NaN and raises the “invalid” floating-point exception for $x < -1$.
- $\log10p1(+\infty)$ returns $+\infty$.

After F.10.4.5, insert the following:

F.10.4.6 The **rsqrt** functions

- **rsqrt**(± 0) returns $\pm\infty$ and raises the “divide-by-zero” floating-point exception.
- **rsqrt**(x) returns a NaN and raises the “invalid” floating-point exception for $x < 0$.
- **rsqrt**($+\infty$) returns +0.

F.10.4.7 The **compoundn** functions

- **compoundn**(x , 0) returns 1 for $x \geq -1$ or x a NaN.
- **compoundn**(x , n) returns a NaN and raises the “invalid” floating-point exception for $x < -1$.
- **compoundn**(-1 , n) returns $+\infty$ and raises the divide-by-zero floating-point exception for $n < 0$.
- **compoundn**(-1 , n) returns +0 for $n > 0$.

F.10.4.8 The **rootn** functions

- **rootn**(± 0 , n) returns $\pm\infty$ and raises the “divide-by-zero” floating-point exception for odd $n < 0$.
- **rootn**(± 0 , n) returns $+\infty$ and raises the “divide-by-zero” floating-point exception for even $n < 0$.
- **rootn**(± 0 , n) returns +0 for even $n > 0$.
- **rootn**(± 0 , n) returns ± 0 for odd $n > 0$.
- **rootn**($\pm\infty$, n) is equivalent to **rootn**(± 0 , $-n$) for n not 0, except that the “divide-by-zero” floating-point exception is not raised.
- **rootn**(x , 0) returns a NaN and raises the “invalid” floating-point exception for all x (including NaN).
- **rootn**(x , n) returns a NaN and raises the “invalid” floating-point exception for $x < 0$ and n even.

F.10.4.9 The **pown** functions

- **pown**(x , 0) returns 1 for all x not a signaling NaN.
- **pown**(± 0 , n) returns $\pm\infty$ and raises the “divide-by-zero” floating-point exception for odd $n < 0$.
- **pown**(± 0 , n) returns $+\infty$ and raises the “divide-by-zero” floating-point exception for even $n < 0$.
- **pown**(± 0 , n) returns +0 for even $n > 0$.
- **pown**(± 0 , n) returns ± 0 for odd $n > 0$.
- **pown**($\pm\infty$, n) is equivalent to **pown**(± 0 , $-n$) for n not 0, except that the “divide-by-zero” floating-point exception is not raised.

F.10.4.10 The **powr** functions

- **powr**(x , ± 0) returns 1 for finite $x > 0$.
- **powr**(± 0 , y) returns $+\infty$ and raises the “divide-by-zero” floating-point exception for finite $y < 0$.
- **powr**(± 0 , $-\infty$) returns $+\infty$.
- **powr**(± 0 , y) returns +0 for $y > 0$.
- **powr**($+1$, y) returns 1 for finite y .

- **powr**(*x*, *y*) returns a NaN and raises the “invalid” floating-point exception for $x < 0$.
- **powr**(± 0 , ± 0) returns a NaN and raises the “invalid” floating-point exception.
- **powr**($+\infty$, ± 0) returns a NaN and raises the “invalid” floating-point exception.
- **powr**(1, $\pm\infty$) returns a NaN and raises the “invalid” floating-point exception.

8 Reduction functions in <math.h>

This clause specifies changes to C11 + TS18661-1 + TS18661-2 + TS18661-3 to include functions that support reduction operations recommended by IEC 60559.

Changes to C11 + TS18661-1 + TS18661-2 + TS18661-3:

After 7.12.13a, insert the following:

7.12.13b Reduction functions

The functions in this subclause should be implemented so that intermediate computations do not overflow or underflow.

Functions computing sums of length $n = 0$ return the value +0. Functions computing products of length $n = 0$ return the value 1 and store the scale factor 0 in the object pointed to by **sfptr**.

7.12.13b.1 The **reduc_sum** functions

Synopsis

```
[1] #include <math.h>
#include <stddef.h>
double reduc_sum(size_t n, const double p[static n]);
float reduc_sumf(size_t n, const float p[static n]);
long double reduc_suml(size_t n,
    const long double p[static n]);
_FloatN reduc_sumfN(size_t n, const _FloatN p[static n]);
_FloatNx reduc_sumfNx(size_t n, const _FloatNx p[static n]);
_DecimalN reduc_sumdN(size_t n, const _DecimalN p[static n]);
_DecimalNx reduc_sumdNx(size_t n,
    const _DecimalNx p[static n]);
```

Description

[2] The **reduc_sum** functions compute the sum of the n members of array **p**: $\sum_{i=0, n-1} p[i]$. A range error may occur.

Returns

[3] The **reduc_sum** functions return the computed sum.

7.12.13b.2 The **reduc_sumabs** functions

Synopsis

```
[1] #include <math.h>
#include <stddef.h>
double reduc_sumabs(size_t n, const double p[static n]);
float reduc_sumabsf(size_t n, const float p[static n]);
long double reduc_sumabsl(size_t n,
    const long double p[static n]);
_FloatN reduc_sumabsfN(size_t n, const _FloatN p[static n]);
_FloatNx reduc_sumabsfNx(size_t n,
    const _FloatNx p[static n]);
_DecimalN reduc_sumabsdN(size_t n,
    const _DecimalN p[static n]);
_DecimalNx reduc_sumabsdNx(size_t n,
    const _DecimalNx p[static n]);
```

Description

[2] The **reduc_sumabs** functions compute the sum of the absolute values of the **n** members of array **p**: $\sum_{i=0,n-1} |p[i]|$. A range error may occur.

Returns

[3] The **reduc_sumabs** functions return the computed sum.

7.12.13b.3 The **reduc_sumsq** functions

Synopsis

```
[1] #include <math.h>
#include <stddef.h>
double reduc_sumsq(size_t n, const double p[static n]);
float reduc_sumsqf(size_t n, const float p[static n]);
long double reduc_sumsql(size_t n,
    const long double p[static n]);
_FloatN reduc_sumsqfN(size_t n, const _FloatN p[static n]);
_FloatNx reduc_sumsqfNx(size_t n,
    const _FloatNx p[static n]);
_DecimalN reduc_sumsqdN(size_t n,
    const _DecimalN p[static n]);
_DecimalNx reduc_sumsqdNx(size_t n,
    const _DecimalNx p[static n]);
```

Description

[2] The **reduc_sumsq** functions compute the sum of squares of the values of the **n** members of array **p**: $\sum_{i=0,n-1} (p[i] \times p[i])$. A range error may occur.

Returns

[3] The **reduc_sumsq** functions return the computed sum.

7.12.13b.4 The `reduc_sumprod` functions

Synopsis

```
[1] #include <math.h>
#include <stddef.h>
double reduc_sumprod(size_t n, const double p[static n],
    const double q[static n]);
float reduc_sumprodf(size_t n, const float p[static n],
    const float q[static n]);
long double reduc_sumprodl(size_t n,
    const long double p[static n],
    const long double q[static n]);
_FloatN reduc_sumprodfN(size_t n, const _FloatN p[static n],
    const _FloatN q[static n]);
_FloatNx reduc_sumprodfNx(size_t n,
    const _FloatNx p[static n],
    const _FloatNx q[static n]);
_DecimalN reduc_sumproddN(size_t n,
    const _DecimalN p[static n],
    const _DecimalN q[static n]);
_DecimalNx reduc_sumproddNx(size_t n,
    const _DecimalNx p[static n],
    const _DecimalNx q[static n]);
```

Description

[2] The **`reduc_sumprod`** functions compute the dot product of the sequences of members of the arrays **`p`** and **`q`**: $\sum_{i=0,n-1} (p[i] \times q[i])$. A range error may occur.

Returns

[3] The **`reduc_sumprod`** functions return the computed sum.

7.12.13b.5 The `scaled_prod` functions

Synopsis

```
[1] #include <math.h>
#include <stddef.h>
#include <stdint.h>
double scaled_prod(size_t n,
    const double p[static restrict n],
    intmax_t * restrict sfptr);
float scaled_prodf(size_t n,
    const float p[static restrict n],
    intmax_t * restrict sfptr);
long double scaled_prodl(size_t n,
    const long double p[static restrict n],
    intmax_t * restrict sfptr);
_FloatN scaled_prodfN(size_t n,
    const _FloatN p[static restrict n],
    intmax_t * restrict sfptr);
_FloatNx scaled_prodfNx(size_t n,
    const _FloatNx p[static restrict n],
    intmax_t * restrict sfptr);
_DecimalN scaled_proddN(size_t n,
    const _DecimalN p[static restrict n],
    intmax_t * restrict sfptr);
_DecimalNx scaled_proddNx(size_t n,
    const _DecimalNx p[static restrict n],
    intmax_t * restrict sfptr);
```

Description

[2] The **scaled_prod** functions compute a scaled product pr of the n members of the array p and a scale factor sf , such that $pr \times b^{sf} = \prod_{i=0, n-1} p[i]$, where b is the radix of the type. These functions store the scale factor sf in the object pointed to by **sfptr**. A domain error occurs if the scale factor is outside the range of the **intmax_t** type. The functions should not cause a range error.

Returns

[3] The **scaled_prod** functions return the computed scaled product pr .

7.12.13b.6 The `scaled_prodsum` functions

Synopsis

```
[1] #include <math.h>
#include <stddef.h>
#include <stdint.h>
double scaled_prodsum(size_t n,
    const double p[static restrict n],
    const double q[static restrict n],
    intmax_t * restrict sfptr);
float scaled_prodsurf(size_t n,
    const float p[static restrict n],
    const float q[static restrict n],
    intmax_t * restrict sfptr);
long double scaled_prodsuml(size_t n,
    const long double p[static restrict n],
    const long double q[static restrict n],
    intmax_t * restrict sfptr);
_FloatN scaled_prodsurfN(size_t n,
    const _FloatN p[static restrict n],
    const _FloatN q[static restrict n],
    intmax_t * restrict sfptr);
_FloatNx scaled_prodsurfNx(size_t n,
    const _FloatNx p[static restrict n],
    const _FloatNx q[static restrict n],
    intmax_t * restrict sfptr);
_DecimalN scaled_prodsurmdN(size_t n,
    const _DecimalN p[static restrict n],
    const _DecimalN q[static restrict n],
    intmax_t * restrict sfptr);
_DecimalNx scaled_prodsurmdNx(size_t n,
    const _DecimalNx p[static restrict n],
    const _DecimalNx q[static restrict n],
    intmax_t * restrict sfptr);
```

Description

[2] The `scaled_prodsum` functions compute a scaled product pr of the sums of the corresponding members of the arrays $\mathbf{p}$ and $\mathbf{q}$ and a scale factor sf , such that $pr \times b^{sf} = \prod_{i=0}^{n-1} (p[i] + q[i])$, where b is the radix of the type. These functions store the scale factor sf in the object pointed to by `sfptr`. A domain error occurs if the scale factor is outside the range of the `intmax_t` type. These functions should not cause a range error.

Returns

[3] The `scaled_prodsum` functions return the computed scaled product pr .